# Characterization, Detection, and Synchronization of Audio-Video Events in *Bharatanatyam Adavu*'s

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Abstract. Bharatanatyam is the most popular form of Indian Classical Dance. Its Adavu's are basic choreographic units of a dance sequence. An Adavu is accompanied by percussion and vocal music and follows a specific rhythmic pattern (Sollukattu). In this paper we first characterize the audio, video, and sync events of Adavu's to succinctly represent the Adavu's. Then we present simple yet effective algorithms to detect audio and video events and measure their synchronization. The audio, video, and sync event detection achieve 94%, 84%, and 72% accuracy respectively. A comparison of our audio event detection against a well-known method by Ellis shows significant improvement. We also create an annotated repository of Sollukattu's and Adavu's for research. There are several applications of the characterization and beat detection including music / music video segmentation, synchronization of the postures with the beats, automatic tagging of rhythm metadata etc. Characterization of events or repository of Bharatanatyam Adavu's has not been attempted before.

**Keywords:** Characterization of Dance Videos, Onset Detection, Beat Detection, Key Posture Detection, Audio-Visual Synchronization

## 1 Introduction

Bharatanatyam is a very popular form of Indian Classical Dance. Adavu's are basic choreographic units of a dance sequence in Bharatanatyam. In an Adavu choreographic movements are accompanied by percussion instruments (Tatta Palahai (wooden stick) – Tatta Kozhi (wooden block), Mridangam, or Tabla) and rhythmic vocal sound (utterances). Optionally, vocal music, various woodwind (Nagaswaram, Flute) or string (Violin, or Veena) instruments also accompany Adavu's. Hence, a performance of the an Adavu is recorded as a multimedia stream comprising audio and video streams (based on the sensor there may be other streams as well). This is, therefore, a combination of video events that are either postures or movements synchronized with audio events that are rhythmic pattern of beats or Taals. The rhythmic patterns (meter) used for Adavu's are called *Sollukattu*'s. Every *Adavu* is performed in sync with a *Sollukattu*. There are  $^{1}$  50 *Adavu*'s each performed with one of the 23 *Sollukattu*'s.

In this paper we first present an in-depth characterization of *Bharatanatyam* performances for representation and processing of its audio as well as video streams. We characterize the *Sollukattu*'s (audio stream) in terms of audio-events comprising beats (and half beats), inter-beat silence, and their periodic structure. *Adavu*'s (video stream) are characterized in terms of Key Postures and their transitions, and movements together defining video-events. Finally, we characterize the synchronization between audio and video events and the associated issues in synchronization to understand the multimedia form of *Bharatanatyam* dance. These characterizations are severally used later to formulate algorithms, design tests and validations and create the basis for solving various choreographic problems.

Computationally we first present an algorithm to detect the beats of *Sol-lukattu*'s. These provide major clues to the audio events. Several work on beat detection, tempo estimation, and beat tracking have been reported in [2], [3], and [4]. These algorithms rely on a common scheme where the system extracts the onset locations from a time-frequency or sub-band analysis of the signal, traditionally using a filter bank or the discrete Fourier transform. Then, a periodicity estimation algorithm finds the rate at which these events occur.

Problem of estimating the meter of a musical piece has been addressed in [8], [7], [13], and [6]. The work by [13], [12] and [6] are based on *Indian Hindusthani & Carnatic Music*. Gulati et. al. [6] extended the two stage comb filter-based approach (originally proposed for double/ triple meter estimation) to septuple meter (such as 7/8 time-signature) and evaluated its performance on a sizable Indian music database. In [12], Sridhar et. al. propose a new algorithm to segment the instrumental and the vocal signals. The frequency components of the signal are determined on the voice signal and then these are mapped onto the *swara* sequence. Srinivasamurthy et. al. [13] present an algorithm that uses a beat similarity matrix and inter onset interval histogram to automatically extract the sub-beat structure and the long-term periodicity of a musical piece. On a manually annotated *Carnatic* music data set the recognition accuracy of the algorithm is shown to be 79.3%.

Here, we develop a simple yet effective onset based [4] algorithm to detect the beats for the polyphonic music signal of *Bharatanatyam Adavu*. The algorithm achieves over 94% accuracy for beat detection for the 23 *Sollukattu*'s for a set of annotated audio streams.

Next we analyze the video for the extent of motion between its sequences of consecutive frames to detect Key Frames (containing Key Postures), Transition Frames and Movements. These provide significant clues to video events. We achieve nearly 84% accuracy for key posture detection for the 50 Adavu's for a set of annotated video streams.

<sup>&</sup>lt;sup>1</sup> Depending on the school of *Bharatanatyam*, the exact set of *Adavu*'s and *Sollukattu*'s may vary.

Finally, to explore the synchronization aspects, we correlate the audio events from *Sollukattu*'s with the video events from *Adavu*'s. There has been variety of work in this area including – audio based video event detection [11], dance synthesis based on visual analysis of human motion and audio analysis of music tempo [9], detection of dance motion structure using motion capture and musical information [10], and audio and video tempo analysis for dance detection [5]. However, there has been no attempt to analyze synchronization in Indian Classical Dance forms. Here, we work on synchronization between beats (audio events) and key frames (video events) for the *Adavu*'s and achieve 72% accuracy of sync.

There has been no systematic research on multimedia streams of *Bharata-natyam Adavu*'s. Hence, there is no comprehensive and annotated data set for it. So we also create an annotated repository of *Sollukattu*'s and *Adavu*'s for research. The data set is created using Kinect XBox (Kinect 1.0). Hence it has depth and skeleton data streams synchronized with RGB stream that can be further used for analysis of specific postures and movements. The data set is captured for all 23 *Sollukattu*'s performed independently by 4 trained music accomplices of dancers. All 50 *Adavu*'s are also recorded using 7 different professionally trained dancers. A part of the data has been annotated by *Bharatanatyam* experts. These have been used for validation of our algorithms and comparison with others in some cases. A selective subset of the data has been published<sup>2</sup> for public use.

There are several applications of the characterization and beat detection including music / music video segmentation, synchronization of the postures with the beats, automatic tagging of rhythm metadata etc. Characterization, beat detection, synchronization, segmentation or repository of *Bharatanatyam Adavu*'s has not been attempted before.

The paper makes three major contributions - characterization of audio and video of *Adavu*'s, algorithms for detection of audio events, video events and their synchronization, and creation of an annotated repository of *Bharatanatyam* data.

The paper is organized as follows. We characterize the multi-modal structure of *Bharatanatyam Adavu*'s in terms of audio, video and sync events in Section 2. Audio event (beat) detection is presented in Section 3 where we first outline the pre-processing, followed by onset detection and subsequent pruning, and beat detection. Video event (motion) detection is presented in Section 4. Estimation of sync is then discussed in Section 5. We conclude in Section 6.

# 2 Characterization of Bharatanatyam Adavu's

#### A Bharatanatyam Adavu consists of:

- 1. Audio Stream: *Sollukattu* or rhythmic music as generated by percussion instrument and vocal sound (utterances).
- 2. Video Stream: Stream of frames each capturing the combination of (a) Position of the legs (*Sthanakam*), (b) Posture of standing (*Mandalam*), (c)

<sup>&</sup>lt;sup>2</sup> Data Repository: http://cse.iitkgp.ac.in/resgrp/hci/

Walking Movement (*Chari*), and (d) Hand Gestures (*Nritta Hastas*) as assumed by the dancer.

3. Synchronization: Position, Posture, Movement and Gesture of an Adavu are performed in synchronization among themselves and in synchronization with the rhythm of the music.

To characterize the above and represent an *Adavu* in a succinct manner, we define a set of events.

#### 2.1 Events of Adavu's

An *Event* denotes the occurrence of an activity (called *Causal Activity*) in the audio or the video stream of an *Adavu*. Further, synchronization (sync) events are defined between multiple events based on temporal constraints. Sync events may be defined jointly between audio and video streams. An event is described by:

- 1. *Category*: The nature of the event based on its origin (source) is called Category. It can be *audio*, *video* or *sync*.
- 2. *Type*: Type relates to the causal activity of an event in a given category. Event types are listed in Table 1 with brief description of respective causal activities.
- 3. Time-stamp / range: The time of occurrence of the causal activity of the event. This is elapsed time from the beginning of the stream and is marked by a function  $\tau(.)$ . Often a causal activity may spread over an interval  $[\tau_s, \tau_e]$  which will be associated with the event. Time-stamp and time range are interchangeably denoted by the  $\tau$  function of the event.

For video events, we use range of video frame numbers  $[\eta_s, \eta_e]$  as the temporal interval. The Kinect video has a fixed rate of 30 fps. Hence, for any event we interchangeably use  $\tau$  or  $\eta$  as is appropriate in a context.

- 4. *Label*: One or more optional labels may be attached to an event annotating details for the causal activity.
- 5. *ID*: Every instance of an event in a stream is distinguishable. These are sequentially numbered (within a specific type of an event) in the temporal order of their occurrence.

#### 2.2 Characterization of Audio

The musical meter<sup>3</sup> of an Adavu is called a Sollukattu. Traditionally, a Tatta Palahai (wooden stick) is periodically struck on a Tatta Kozhi (wooden block) in the rhythmic pattern of Adi or Rupak Taal's<sup>4</sup> to produce the periodic beats (or  $\alpha^{fb}$  events). Usually beats repeat in a bar<sup>5</sup> of  $\lambda = 6$  or 8. The tempo of a

<sup>&</sup>lt;sup>3</sup> The *meter* of music is its rhythmic structure.

<sup>&</sup>lt;sup>4</sup> Taal is the Indian system for organizing and playing metrical music.

<sup>&</sup>lt;sup>5</sup> A bar (or measure) is a segment of time corresponding to a specific  $\lambda$  number of beats. Sollukattu's also use longer bars (12, 16, 24, or 32).

Event	Event	Event	Event
Category	Type	Description	Label
Audio	$\alpha^{fb}$	Full beat with <i>bol</i>	$bol^1$ , downbeat <sup>2</sup> , upbeat <sup>3</sup>
Audio	$\alpha^{hb}$	Half beat with <i>bol</i>	bol
Audio	$\alpha^{fn}$	Full beat having no bol	upbeat
Audio	$\alpha^{hn}$	Half beat having no $bol$	
Audio	$\alpha^{qn}$	Quarter <sup>4</sup> beat having no $bol$	
Audio	$\alpha^{sl}$	Silence – No beat or <i>bol</i>	upbeat
Audio	$lpha^f$	$\alpha^{fb} \mid \alpha^{fn}$	$bol^1$ , downbeat <sup>2</sup> , upbeat <sup>3</sup>
Audio	$\alpha^h$	$\alpha^{hb} \mid \alpha^{hn}$	bol
Audio	$\alpha$	$\alpha^f \mid \alpha^h \mid \alpha^{qn} \mid \alpha^{sl}$	
		5	7
Video	$\nu^{nm}$	No motion <sup>o</sup>	Range of Frames <sup>o</sup> , Key Posture <sup>'</sup>
Video	$\nu^{\iota r}$	Transition Motion <sup>°</sup>	Range of Frames
Video	$\nu^{tj}$	Trajectory Motion <sup>9</sup>	Range of Frames, Trajectory
Video	$ u^t$	$ u^{tr} \mid v^{tj}$	Range of Frames, Trajectory
Video	u	$ u^t \mid v^{nm}$	
Sync	$\psi^{fb}$	No motion @ Full beat <sup>10</sup>	Key Posture
Sync	$\psi^{hb}$	No motion @ Half beat	Key Posture
Sync	$\psi$	$ \psi^{fb}  \psi^{hb}$	

Table 1. List of Events in Bharatanatyam Adavu's

1: Vocalized *bol*'s accompany some beats

2: The first beat of a bar

3: The last beat in the previous bar which immediately precedes, and hence anticipates, the downbeat

4: Sollukattu's do not use quarter beats to define a meter. However, often

the beat player would produce one that needs to be ignored 5: Frames over which the dancer does not move (assumes a Kev Posture)

6: Sequence of consecutive frames over which the events spreads

5. Sequence of consecutive frames over which the events spread

7: A Key Posture is a well-defined and stationery posture

8: Transitory motion to change from one Key Posture to the next. This has no well-defined trajectory of movement for limbs

9: Motion that follows a well-defined trajectory of movement for limbs

10:  $\alpha^{fb}$  and  $\nu^{nm}$  in sync. That is,  $\tau(\alpha^{fb}) \cap \tau(\nu^{nm}) \neq \phi$ 

meter is measured by beats per minute (bpm). We use Period T = (60/bpm) or the time interval between two consecutive beats in secs as the temporal measure for a meter.

Consider two consecutive beats  $\alpha_i^{fb}$  and  $\alpha_{i+1}^{fb}$  in a bar of  $\lambda$ , where *i* denotes the  $i^{th}$   $(1 \leq i < \lambda)$  period. The time-stamps of the respective events are then related as  $\tau(\alpha_{i+1}^{fb}) - \tau(\alpha_i^{fb}) \approx T$ . Further the bar repeats after an equal time interval of *T*. That is,  $\tau(\alpha_{\lambda*i+1}^{fb}) - \tau(\alpha_{\lambda*i}^{fb}) \approx T$ ,  $i \geq 1$ . We refer to such beats as *full beats* and hence the superscript fb in  $\alpha^{fb}$  events. The first beat  $\alpha_1^{fb}$  (last beat  $\alpha_{\lambda}^{fb}$ ) of a bar is referred to as a *downbeat* (*upbeat*). We mark these on the events as labels.

In many *Sollukattu*'s beating is also performed at the middle of a period. These are called *half beats* and produce the  $\alpha_i^{hb}$  events in the  $i^{th}$  period. Naturally,  $\tau(\alpha_i^{hb}) - \tau(\alpha_i^{fb}) \approx \tau(\alpha_{i+1}^{fb}) - \tau(\alpha_i^{hb}) \approx T/2.$ 

A Sollukattu uses one of the 3 different speeds or Tempo (Laya) - Vilambit Laya (Slow), Madhya Laya (Medium), and Drut Laya (High). The Period (T) depends on the Tempo (shorter for faster tempo) and remains more or less uniform across Sollukattu's.

Often in a *Sollukattu* an accomplice of the dancer also speaks out a distinct vocalization of rhythm with words like *tat*, *tei*, *ta* etc., called *Bol*'s. These are done in sync with a full beat or a half beat. We represent *bol*'s as labels of the respective  $\alpha^{fb}$  or  $\alpha^{hb}$  events. A *bol* is optional for an event.

There are 23 *Sollukattu*'s. We illustrate a few here to understand various meters. All *Sollukattu*'s are shown in *Vilambit Laya*.

- 1. Kuditta Mettu ( $T \approx 1.2$  secs,  $\lambda = 8$ ): We show two meters of it in Table 2 and Figure 1 (a). Note that it has only  $\alpha^{fb}$  events.
- 2. Tatta\_C Sollukattu ( $T \approx 1.6$  secs,  $\lambda = 8$ ): It has  $\alpha^{fb}$  as well as  $\alpha^{hb}$  events (Table 3 and Figure 1 (b)).
- 3. Kuditta Nattal\_A & Tatta\_E ( $T \approx 1.0 \text{ secs}, \lambda = 8$ ): In addition to  $\alpha^{fb}, \alpha^{fn}$  and  $\alpha^{hn}$  events are also found (Table 4) where there is only beating and no bol.
- 4. Joining\_B ( $T \approx 1.5 \text{ secs}, \lambda = 8$ ): As such it uses only  $\alpha^{fb}$ 's (Table 4). But the 4<sup>th</sup> and 8<sup>th</sup> beats are silent ( $\alpha^{sl}$ ) with neither any bol nor any beating. So the upbeat in this case is guessed from T.

#### 2.3 Characterization of Video

While performing an Adavu the dancer closely follows the beats of the accompanying<sup>6</sup> Sollukattu and synchronizes her movements with the beats. At a beat, the dancer assumes a Key Posture<sup>7</sup> and holds it for a little while before quickly changing to the next Key Posture at the next beat. Consequently, while the dancer holds the key posture, she stays almost stationary and there is no or very slow motion in the video. This leads to  $\nu^{nm}$  (no-motion) events. Further, while the dancer changes to the next key posture, we observe the  $\nu^{tr}$  (transition) or  $\nu^{tj}$  (trajectory) motion events. Since a frame is an atomic observable unit in a video, we can classify the frames of the video of an Adavu into 2 classes:

<sup>&</sup>lt;sup>6</sup> Every *Adavu* is performed with a specific *Sollukattu*. In this paper, we use 50 *Adavu*'s each performed with one of 23 *Sollukattu*'s.

<sup>&</sup>lt;sup>7</sup> A *Key Posture* is defined in terms of Position of the legs (*Sthanakam*) and Posture of standing (*Mandalam*). Some are laterally symmetric ((c)–(h) in Figure 2), while rest have *left* and *right* sided variants ((a)–(b)).

Event	Time	Gap	Event	Time	Gap
	$(\tau_i)$	$(\tau_i - \tau_{i-1})$		$(\tau_i)$	$(\tau_i - \tau_{i-1})$
$\alpha_1^{fb}(\text{tei})$	2.681		$\alpha_9^{fb}$ (tei)	12.271	1.207
$\alpha_2^{fb}(\mathrm{hat})$	3.912	1.231	$\alpha_{10}^{fb}(\text{hat})$	13.386	1.115
$\alpha_3^{fb}(\text{tei})$	5.108	1.196	$\alpha_{11}^{fb}$ (tei)	14.512	1.126
$\alpha_4^{fb}(\text{hi})$	6.269	1.161	$\alpha_{12}^{fb}(\text{hi})$	15.603	1.091
$\alpha_5^{fb}(\text{tei})$	7.523	1.254	$\alpha_{13}^{fb}(\text{tei})$	16.764	1.161
$\alpha_6^{fb}(\mathrm{hat})$	8.742	1.219	$\alpha_{14}^{fb}(\text{hat})$	17.902	1.138
$\alpha_7^{fb}$ (tei)	9.891	1.149	$\alpha_{15}^{fb}$ (tei)	19.028	1.126
$\alpha_8^{fb}(hi)$	11.064	1.173	$\alpha_{16}^{fb}(\text{hi})$	20.178	1.150

**Table 2.** Pattern of *Kuditta Mettu Sollukattu* (Figure 1 (a)) annotated with timestamps  $\tau_i$  (start-time of the full beat event  $\alpha^{fb}$ ).  $Gap_i = \tau_i - \tau_{i-1}$  is computed from consecutive time-stamps and provides the distribution for tempo period T

**Table 3.** Pattern of *Tatta\_C Sollukattu* (Figure 1 (b)) annotated with time-stamps  $\tau_i$  (start-time of the full-beat event  $\alpha^{fb}$ ).  $Gap_i = \tau_i - \tau_{i-1}$  is computed from consecutive time-stamps and provides the distribution for tempo period *T*. Half-beat offsets happen roughly at T/2.

Event	Time	Gap	1/2-Beat	Event	Time	Gap	1/2–Beat
	$(\tau_i)$	$(\tau_i - \tau_{i-1})$	Offset		$(\tau_i)$	$(\tau_i - \tau_{i-1})$	Offset
$\alpha_1^{fb}(\text{tei})$	6.571			$\alpha_5^{fb}$ (tei)	13.003	1.64	
$\alpha_1^{hb}(ya)$	7.395		0.82	$\alpha_5^{hb}(ya)$	13.815		0.81
$\alpha_2^{fb}(\text{tei})$	8.185	1.61		$\alpha_6^{fb}$ (tei)	14.628	1.63	
$\alpha_2^{hb}(ya)$	8.962		0.78	$\alpha_6^{hb}(\rm ya)$	15.441		0.81
$\alpha_3^{fb}$ (tei)	9.752	1.57		$\alpha_7^{fb}$ (tei)	16.184	1.56	
$\alpha_3^{hb}(ya)$	10.565		0.81	$\alpha_7^{hb}(ya)$	17.031		0.85
$\alpha_4^{fb}$ (tei)	11.366	1.61		$\alpha_8^{fb}$ (tei)	17.809	1.63	

- 1. *K-frame's* or Key Frames: These frames contain key postures where the dancer *holds* the Posture. Evidently, a  $\nu^{nm}$  has the sequence of *K-frames* as labels. All *K-frames* of an  $\nu^{nm}$  contain the same key posture.
- 2. **T-frame's of Transition Frame**: These are transition frames between two *K*-frames while the dancer is rapidly changing posture to assume the next key posture from the previous one. A  $\nu^{tr}$  or  $\nu^{tj}$  event has a sequence of *T*-frames as labels.

For an *Aadvu* the transition can either be performed according to a welldefined trajectory<sup>8</sup> for the hands and legs or may just be undefined and arbitrary. Former is defined as  $\nu^{tj}$  events and the latter is marked as  $\nu^{tr}$ 

<sup>&</sup>lt;sup>8</sup> In Bharatanatyam, these could be various forms of Nritta (rhythmical and repetitive elements) like Chari, Karana, Angahara or Mandala.

Sollukattu	Description of Bol / Adavus
Kuditta	$\alpha_1^{fb}(\text{tei}) \ \alpha_2^{fb}(\text{hat}) \ \alpha_3^{fb}(\text{tei}) \ \alpha_4^{fb}(\text{hi}) \ \alpha_5^{fb}(\text{tei}) \ \alpha_6^{fb}(\text{hat}) \ \alpha_7^{fb}(\text{tei}) \ \alpha_8^{fb}(\text{hi})$
Mettu	Adavu: Kuditta_Mettu 1, 2, 3, 4
Kuditta	$\alpha_1^{fb}(\text{tat}) \ \alpha_2^{fb}(\text{tei}) \ \alpha_2^{hn} \ \alpha_3^{fb}(\text{tam}) \ \alpha_4^{fn} \ \alpha_4^{hn} \ \alpha_5^{fb}(\text{dhit}) \ \alpha_6^{fb}(\text{tei}) \ \alpha_6^{hn} \ \alpha_7^{fb}(\text{tam}) \ \alpha_8^{fn} \ \alpha_8^{hn}$
Nattal A	Adavu: Kuditta_Nattal 1, 2, 3, 6
Tatta E	$\alpha_1^{fb}(\text{tei}) \ \alpha_2^{fb}(\text{tei}) \ \alpha_3^{fb}(\text{tam}) \ \alpha_4^{fn} \ \alpha_4^{hn} \ \alpha_5^{fb}(\text{tei}) \ \alpha_6^{fb}(\text{tei}) \ \alpha_7^{fb}(\text{tam}) \ \alpha_8^{fn} \ \alpha_8^{hn}$
	Adavu: Tatta 6
Joining B	$\alpha_1^{fb}(\text{dhit}) \ \alpha_2^{fb}(\text{dhit}) \ \alpha_3^{fb}(\text{tei}) \ \alpha_4^{sl} \ \alpha_5^{fb}(\text{dhit}) \ \alpha_6^{fb}(\text{dhit}) \ \alpha_7^{fb}(\text{tei}) \ \alpha_8^{sl}$
	Adavu: Joining 2

Table 4. Variations in the patterns of Sollukattu's with Adavu's

event. In this paper we do not deal with trajectory-based motion and hence do not distinguish between  $\nu^{tj}$  and  $\nu^{tr}$  events.

In Figure 2 we show the key postures of *Kuditta Mettu Adavu* at every beat of the first bar of *Kuditta Mettu Sollukattu*. The corresponding video and audio events are marked in Table 5 with K-/T-Frames. These are also marked on the *Sollukattu* in Figure 1(a). Note that only the right-sided half of the postures are shown.

Events	K-/T-F	rames	Events	K-/T-Frame	
	Range	# of		Range	# of
$\nu_1^{nm} \left[ \alpha_1^{fb}(\text{tei}) \right]$	70–99	30	$\nu_9^{nm} \left[ \alpha_9^{fb}(\text{tei}) \right]$	359–386	28
$\nu_1^{tr}$	100 - 103	4	$ u_9^{tr}$	387-390	4
$\nu_2^{nm}  \left[ \alpha_2^{fb}(\text{hat}) \right]$	104 - 124	21	$\nu_{10}^{nm}  \left[ \alpha_{10}^{fb}(\text{hat}) \right]$	391 - 410	20
$\nu_2^{tr}$	125 - 145	21	$ u_{10}^{tr}$	411 - 429	19
$\nu_3^{nm} \left[ \alpha_3^{fb}(\text{tei}) \right]$	146 - 172	27	$\nu_{11}^{nm} \left[ \alpha_{11}^{fb}(\text{tei}) \right]$	430 - 451	22
$\nu_3^{tr}$	173 - 176	4	$ u_{11}^{tr}$	452 - 455	4
$\nu_4^{nm} \left[ \alpha_4^{fb}(\mathrm{hi}) \right]$	177 - 191	15	$\nu_{12}^{nm}  \left[ \alpha_{12}^{fb}(\text{hi}) \right]$	456 - 470	15
$ u_4^{tr}$	192 - 214	23	$ u_{12}^{tr} $	471 - 492	22
$\nu_5^{nm} \left[ \alpha_5^{fb}(\text{tei}) \right]$	215 - 245	31	$\frac{\nu_{13}^{nm}}{\nu_{13}^{nm}} \left[\alpha_{13}^{fb}(\text{tei})\right]$	493 - 521	29
$\nu_5^{tr}$	246 - 249	4	$\nu_{13}^{tr}$	522 - 525	4
$\nu_6^{nm} \ [\alpha_6^{fb}(\text{hat})]$	250 - 262	13	$\nu_{14}^{nm}  \left[ \alpha_{14}^{fb}(\mathrm{hat}) \right]$	526 - 542	17
$\nu_6^{tr}$	263 - 287	25	$ u_{14}^{tr}$	543 - 564	22
$\nu_7^{nm} \left[ \alpha_7^{fb} (\text{tei}) \right]$	288 - 314	27	$\nu_{15}^{nm} \left[ \alpha_{15}^{fb}(\text{tei}) \right]$	565 - 587	23
$\nu_7^{tr}$	315 - 317	3	$ u_{15}^{tr}$	588 - 590	3
$\nu_8^{nm}  \left[ \alpha_8^{fb}(\text{hi}) \right]$	318-345	28	$\nu_{16}^{nm}  \left[ \alpha_{16}^{fb}(\text{hi}) \right]$	591 - 620	30
$\nu_8^{tr}$	346-358	13	$\nu_{16}^{tr}$	621 -	_

Table 5. Patterns of Kuditta Mettu Adavu (Figure 2)



Fig. 1. Marking of beats and annotations of *bol*'s for 2 bars and  $\lambda = 8$ . Full beat  $(\alpha^{fb})$  and half beat  $(\alpha^{hb})$  event positions are highlighted and corresponding *bol*'s and timestamps are shown (Tables 2 & 3). Note that several  $\alpha^{hn}$  and  $\alpha^{qn}$  events are visible in the signals. These are rather incidental and not intended in the *Sollukattu*. Also, the beatings before the downbeat  $(\alpha_1^{fb})$  are ignored. (a) *Kuditta Mettu Sollukattu* (T = 1.16sec.). Right-sided *Key Postures* (Figure 2) are also shown for the first 8 beats. Leftsided *Key Postures* are performed for the next 8 beats. (b) *Tatta\_C Sollukattu* (T = 1.56sec.).



**Fig. 2.** Right-sided Key Postures of *Kuditta Mettu Adavu* (Variant = 2, *Sollukattu = Kuditta Mettu*) with *Bol*'s for Bar 1. From a *tei* to the next *hat* or *hi* the dancer sharply lowers her raised feet. Further, 8 left-sided Key Postures are performed for the next 8 beats in Bar 2.

#### 2.4 Characterization of Synchronization

A Bharatanatyam dancer intends to perform the key postures of an Adavu in synchronization with the beats. Hence audio events like  $\alpha^{fb}$  and corresponding video events like  $\nu^{nm}$  should be in sync. Every Adavu has a well-defined set of rules that specifies this synchronization based on its associated Sollukattu. For example, in Figure 2, we show how different key postures should be assumed in the Kuditta Mettu Avadu at every beat of the Kuditta Mettu Sollukattu. That is, how the  $\alpha^{fb}$ 's of a bar in the audio should sync with the  $\nu^{nm}$ 's of the video. Other Adavu's require several other forms of synchronization between the audio-video events including sync between beats and trajectory-based body movements  $\nu^{tj}$ .

We assert a sync event  $\psi^{fb}$  if a key posture  $(\nu^{nm})$  sync with a corresponding (full) beat  $(\alpha^{fb})$ . In simple terms, a  $\psi^{fb}$  occurs if the time intervals of  $\alpha^{fb}$  and  $\nu^{nm}$  events overlap. That is,  $\tau(\psi^{fb}) = \tau(\alpha^{fb}) \cap \tau(\nu^{nm}) \neq \phi$ . Similar sync events may be defined between other audio and video events according to the rules of A davu's.

Perfect synchronization is always intended and desirable for a performance. However, we often observe the lack of it due to various reasons. The beating instrument, vocal *bol*'s, and body postures each has a different latency. If a posture is assumed *after hearing* the beat,  $\nu^{nm}$  will lag  $\alpha^{fb}$ . If the dancer assumes the posture in *anticipation*,  $\nu^{nm}$  may lead  $\alpha^{fb}$ . Lack of sync may also arise due to imperfect performance of the dancer, the beater, the vocalist, or a combination of them. Hence, analysis and estimation of sync is critical for processing *Adavu*.

While sync between the audio and video streams is fundamental to the choreography, there are a variety of other synchronization issues that need to be explored. These include sync between beats of beating (instrumental) and (vocalized) *bol*'s, uniformity of time gap between consecutive beats, sync between different body limbs while changing from one key posture to the next, and so on.

Based on the characterizations, we next present algorithms for detection of select audio, video and sync events. In the rest of the paper, we focus only on  $\alpha^{fb}$ ,  $\nu^{nm}$ ,  $\nu^{tr}$  and  $\psi^{fb}$  events.

## 3 Audio Event Detection

We detect the beats in *Sollukattu*'s in four steps as follows:

#### 3.1 Pre-processing of the Audio Signal Sollukattu

A *Sollukattu* is a mixture of two sources of sound – percussion and vocal – that are synchronized by generation. It has dominant frequencies and is periodic. But it is cluttered with a lot of harmonics. So to eliminate the harmonics and noise to estimate the periodicity, we analyze it in frequency domain.

Considering N samples in the signal S(t), we compute its FFT as  $S^*(f)$ . The frequency components in  $S^*(f)$  ranges from 0 to 8 KHz with up to 800Hz contributing to vocal sound (*Bol's*) and 1kHz to 2.6kHz to percussion sound (beating stick). Rest are harmonics.

Hence, we filter  $S^*(f)$  restricting between 1Hz to 2.6kHz to eliminate the vocal sound and the harmonics and get  $S_{filt}^*(f)$ . Inverse FFT of  $S_{filt}^*(f)$  gives  $S_{filt}(t)$ . Usually, the beats have high amplitude. So we discard the low amplitude components in  $S_{filt}(t)$  by a threshold Th = 0.5 to get  $S_{Th}(t)$ . This is used for onset detection.

#### 3.2 Detection of Onsets

From  $S_{Th}(t)$  we compute the Onset Strength Envelope using [4].  $S_{Th}(t)$  is resampled at 8kHz, and STFT<sup>9</sup> (spectrogram) is calculated using 32ms windows and 4ms advance between frames. It is first mapped to 40 Mel bands via a weighted sum of the spectrogram values and then the Mel spectrogram is converted to dB. The first order difference along time is calculated in each band. Negative values are set to zero (half wave rectification) and, positive differences are summed up across all frequency bands. Finally, the signal is passed through a high-pass filter with a cut-off around 0.4Hz to make it locally zero-mean, and then is smoothed by convolving with a Gaussian envelope of about 20ms width. The output is the OSE as a function of time that responds to proportional increase in energy summed across approximately auditory frequency bands. The algorithm also outputs the onset time in the audio stream.

<sup>&</sup>lt;sup>9</sup> Short-Time Fourier Transform

## 3.3 Detection of Local Maxima

Naturally, every beat has an onset in the OSE, but every onset in OSE is not necessarily a beat. An onset is associated with a beat only if it is a local maxima in the OSE. To model the locality we use a window of time interval  $T_w$ , slide it over the OSE and compute the set of local maxima  $L_{max}$  at every time position in OSE. This is given in Algorithm 1.  $L_{max}$  may have more than one local maxima in a window. So in Algorithm 2 we prune the set of onsets in  $L_{max}$  to ensure that only one onset can be present in a window  $T_w$ . Pruned  $L_{max}$  contains the candidates for detected beats.

Algorithm 1 : Local Maxima Detection

1: Inputs: 2:  $O_t =$ Vector of detected onset times,  $nOnset = length(O_t);$ 3:  $Val_t =$ Strength of onsets in  $O_t$ ; 4:  $T_w$  = Window of time interval for local maxima, a threshold parameter; 5: Output: 6:  $L_{max}$  = Vector containing the indices of the locally maximal onsets 7: for i = 1 : nOnset do 8:  $L_{max}(i) = 0;$ 9: end for 10: for i = 1 : nOnset do 11: max = i: 12:for do j = i + 1 : nOnset13:if  $O_t(i) - O_t(j) < T_w$  then if  $Val_t(j) > Val_t(max)$  then 14:max = j;15:16:end if 17:else 18:break; 19:end if 20:end for 21:  $L_{max}(max) = 1;$ 22: end for

#### 3.4 Beat Detection

Using  $L_{max}$  and the periodicity of the *Sollukattu*'s we detect and mark the beats in Algorithm 3. The first candidate beat is detected as the downbeat<sup>10</sup>. For every detected beat *beat<sub>d</sub>*, we search for the next beat from  $L_{max}$  that lie within *period<sub>low</sub>* and *period<sub>high</sub>* from *beat<sub>d</sub>*, where *period<sub>low</sub>* and *period<sub>high</sub>* are global bounds on the tempo period of the *Sollukattu*'s at given speed (*laya*) and are considered invariant. We also use a threshold period *period<sub>th</sub>* which is slightly

<sup>&</sup>lt;sup>10</sup> The first beat of the *Sollukattu*.

Algorithm 2 : Prunning of Local Maxima

1: Inputs:  $O_t$ ,  $Val_t$ ,  $T_w$ ,  $L_{max}$  = Vector containing the indices of the locally maximal onsets 2: Output: 3:  $L_{max}$  = Vector containing the pruned indices of the locally maximal onsets 4: for  $i = 1 : length(L_{max}) - 1$  do if  $L_{max}(i) == 1$  then 5:6: for  $j = i + 1 : length(L_{max})$  do 7:if  $L_{max}(j) == 1$  then 8: if  $O_t(i) - O_t(j) < T_w$  then if  $Val_t(i) > Val_t(j)$  then 9: 10:  $L_{max}(j) = 0;$ 11:else  $L_{max}(i) = 0;$ 12:end if 13:14:end if 15:end if 16:end for end if 17:18: end for

## Algorithm 3 : Beat Detection

1: Inputs: 2:  $L_{max}$  = Vector containing the pruned indices of the locally maximal onsets 3:  $period_{max} = Maximum$  tempo period for any Sollukattu 4:  $period_{min}$  = Minimum tempo period for any Sollukattu 5:  $period_{th} = Threshold tempo period, period_{th} > period_{max}$ . Typically  $period_{th} = 2$ . 6: Output: 7: Beats = Vector containing the indices of the detected beats 8:  $Beats(1) = L_{max}(1);$ 9: i = 1; 10: for  $ind = 2 : length(L_{max})$  do if  $L_{max}(ind) - Beats(i) > period_{min}$  then 11: 12:if  $L_{max}(ind) - Beats(i) < period_{max}$  then i = i + 1;13:14: $Beats(i) = L_{max}(ind);$ else  $L_{max}(ind) - Beats(i) > period_{th}$ 15:16:i = i + 1; $Beats(i) = L_{max}(ind);$ 17:end if 18:end if 19:20: end for

more than  $period_{high}$ . If no beat is found in  $L_{max}$  within  $period_{high}$  of  $beat_d$  then the next beat in  $L_{max}$  that is away by  $period_{th}$  or more is detected. This is done to avoid missing a beat.

We illustrate the working of the algorithm in Table  $\frac{6}{6}$  for *Kuditta Mettu* by striking out onsets in successive stages.

**Table 6.** Illustration of steps for beat detection in *Kuditta Mettu Sollukattu*. We use  $T_w = 0.6$  sec.,  $period_{max} = 1.6$  sec.,  $period_{min} = 1.2$  sec.,  $period_{th} = 2.0$  sec.  $T_{anno}$  shows the set of time-stamps in annotation. These are used as reference for validation.

Bol	tei	hat	tei	hi	tei	hat	tei	hi	tei	hat	tei	hi	tei	hat	tei	hi
$T_{anno}$	2.68	3.91	5.11	6.27	7.52	8.74	9.89	11.06	12.27	13.39	14.51	15.60	16.76	17.90	19.03	20.18
OSE	2.69	4.00	5.15	6.28	7.53	8.75	9.90	11.08	12.34	13.49	14.52	15.62	16.77	17.99	19.03	20.19
	2.76	4.80		6.35		<del>8.83</del>		$\frac{11.15}{11.15}$		13.95		$\frac{15.69}{15.69}$		18.47	19.09	$\frac{20.26}{20.26}$
				6.88		9.60		11.68		14.22		16.17		18.75		
				7.21				11.98								
L <sub>max</sub>	2.69	4.00	5.15	6.28	7.53	8.75	9.90	11.08	12.34	13.49	14.52	15.62	16.77	17.99	19.03	20.19
	2.76	4.80		6.88		9.60		11.68		$\frac{13.95}{1}$		16.17		18.47	19.09	
								$\frac{11.98}{11.98}$		14.22						
L <sub>max</sub>	2.69	4.00	5.15	6.28	7.53	8.75	9.90	11.08	12.34	13.49	14.52	15.62	16.77	17.99	19.03	20.19
(pruned)	$\frac{2.76}{2.76}$	4.80		<del>6.88</del>		9.60		11.68				$\frac{16.17}{16.17}$			19.09	
Beats	2.69	4.00	5.15	6.28	7.53	8.75	9.90	11.08	12.34	13.49	14.52	15.62	16.77	17.99	19.03	20.19

#### 3.5 Results of Audio Event Detection

Now we present the beat detection results and compare our algorithm with the well-known algorithm of Ellis [4] using our recorded data set.

Audio Data Set: Recorded audio data of *Sollukattu*'s are not available for research. Hence we have created a benchmark data set with the help of performers from a dance school<sup>11</sup>.

Sollukattu's have been recorded by Zoom H2n Portable Handy Recorder. For each of the 23 Sollukattu's we have recorded 6 sets performed by 4 (3 female and 1 male) accomplices. Of these, two sets have so far been annotated (sample annotations are shown in Tables 2, 3, 6 and 8) by experts by marking every beat in the audio file as a range of time-stamp of its occurrence. The accompanying bol for every beat is also annotated. One of the annotated sets<sup>12</sup> is taken as the golden audio and used for the recording of the videos.

**Result Analysis:** We now present the results of beat detection in Table 7 for all *Sollukattu*'s using the annotated set. For the  $i^{th}$  annotated beat event<sup>13</sup>  $\alpha_a^i$ 

<sup>&</sup>lt;sup>11</sup> Natanam Kalakshetra, Kolkata, India

<sup>&</sup>lt;sup>12</sup> This data set is available at: http://cse.iitkgp.ac.in/resgrp/hci/

<sup>&</sup>lt;sup>13</sup> We consider only  $\alpha^f \mid \alpha^h$ 

in Sollukattu s, let the time range be  $[\tau_b(\alpha_a^i), \tau_e(\alpha_a^i)]$  and let the corresponding detected beat be  $\alpha_d^i$  with time-stamp  $\tau(\alpha_d^i)$ . The error in detected time is defined as  $\epsilon_i = \tau(\alpha_d^i) - \tau_b(\alpha_a^i)$ . The Absolute Error is defined as  $E_{abs}^i = |\epsilon_i|$  and the Relative Error is defined as  $E_{rel}^i = E_{abs}^i/T$ , where T is the tempo period of s. If s has n beats in its bar, then we define the following error metrics for accuracy:

- 1.  $Max(s) = \max_{i=1}^{n} E_i$
- 2.  $85_{ptl}(s) = 85$  percentile in  $E_i, 1 \le i \le n$ . That is, 85% of the errors are less than  $85_{ptl}(s)$ .
- 3.  $Median(s) = median_{i=1}^{n} E_i$ . That is, half of the errors are less than Median(s).

where  $E_i = E_{abs}^i$  or  $E_{rel}^i$ .

**Table 7.** Result of beat detection for all *Sollukattu*'s using  $T_w = 0.6$  sec.,  $period_{max} = 1.6$  sec.,  $period_{min} = 1.2$  sec.,  $period_{th} = 2.0$  sec.. We compute several statistics for  $E_{abs}$  and  $E_{rel}$  for analysis. The absolute error  $E_{abs}$  as the difference between the annotated and detected time of a beat. Relative error  $E_{rel}$  is computed as a percentage of the period of the *Sollukattu*.

				$E_{abs}$			$E_{rel}$		]
Sr.	Sollukattu	Tempo	Max	$85_{ptl}$	Med-	Max	$85_{ m ptl}$	Med-	Remarks
No.		Period			ian			ian	
1	Joining A	1.18	0.13	0.11	0.02	11	9	2	
2	Joining B	1.52	0.12	0.11	0.01	8	7	1	
3	Joining C	1.17	0.12	0.01	0.01	10	1	1	
4	Kartari Utsanga	1.07	0.15	0.11	0.05	14	10	5	
5	Kuditta Mettu	1.16	0.11	0.08	0.01	9	7	1	
6	Kuditta Nattal A	0.99	0.28	0.06	0.01	29	6	1	2 outliers
7	Kuditta Nattal B	1.30	0.08	0.07	0.05	6	5	4	
8	Kuditta Tattal	1.21	0.22	0.05	0.01	18	4	1	
9	Natta	1.39	0.08	0.07	0.01	6	5	1	
10	Paikkal	1.58	0.12	0.10	0.07	8	6	4	
11	Pakka	1.21	0.50	0.13	0.10	41	11	8	1 outlier
12	Sarika	0.93	0.15	0.05	0.03	16	6	3	
13	Tatta A	1.51	0.39	0.38	0.10	26	25	6	2 outliers
14	Tatta B	1.36	0.06	0.05	0.03	5	4	2	
15	Tatta C	1.56	0.13	0.13	0.07	9	8	4	
16	Tatta D	1.35	0.16	0.14	0.11	12	10	8	7 outliers
17	Tatta E	1.17	0.53	0.14	0.04	$\underline{45}$	12	3	1 outlier
18	Tatta F	1.21	0.15	0.13	0.05	13	10	4	
19	Tatta G	1.32	0.24	0.20	<u>0.13</u>	18	<u>15</u>	10	6 outliers
20	Tei Tei Dhatta	1.41	0.12	0.11	0.06	8	8	4	
21	Tirmana A	1.23	0.04	0.04	0.01	4	3	1	
22	Tirmana B	1.22	0.10	0.09	0.04	8	8	3	
23	Tirmana C	1.46	0.41	0.33	0.02	28	22	1	2 outliers

We compute the above error metrics for  $E_{abs}$  and  $E_{rel}$  in Table 7. Using 0.25 sec., 0.15 sec., and 0.10 sec. as cutoffs respectively for Max,  $85_{ptl}$  and Median,

we have marked outlier measures in the table with underline. On the detected beats also we have computed the outliers for these values and summarized their number under the *Remarks* column. There are 21 outliers in detection of 377 beats in total. Hence, 356 beats are detected correctly. So we achieve an accuracy of 94%.

It may be noted that 13 of the 21 outliers come from Tatta D and Tatta G. This is due to higher variation of inter-beat time in these cases. As expected, more outliers are observed when the inter-beat times vary more widely.

Next we compare the accuracy of our results against the algorithm by Ellis [4].

**Comparison with Ellis'** [4] **Algorithm:** In Table 8, we compare the results of beat detection for *Pakka Sollukattu* by our method against [4] by computing the recall and precision in each case. Ellis' method achieves 100% recall at only 25% precision, while our method achieves 97% recall at 97% precision. However, this comparison is not exactly apple-to-apple because Ellis' method estimates the tempo period from the signal (during the dynamic programming stage) while we use a preset range of tempo periods and a tempo threshold (Algorithm 3).

So in Table 9 we study the accuracy of the estimation of tempo period that Ellis' method performs internally. The method makes two guesses for *Slower* and *Faster* tempo (in terms of *bpm*) and uses a *Strength* parameter for the final choice. If *Strength* < 0.5, it chooses the *Faster* tempo, else it chooses the *Slower*. Out of 23 cases, it gets the tempo period right in only 5 cases and hence the beat detection results degrade.

Finally, we tweak the algorithm of Ellis by inputting the correct tempo period for detecting the beats. We then compare the recall and precision of Ellis' method (with estimated as well as given tempo period) and our method (given a global range of tempo periods) in Table 10. We find that given the tempo period, the precision of Ellis' method improves (or remains same) in 22 cases (96%) while the recall degrades in 15 cases (65%). Our method has a better (or equal) precision in 18 cases (78%) and a better (or equal) recall in 19 cases (83%). Overall we achieve more than 80% precision for over 80% recall in 19 cases (83%). So we do better in terms of our pruning and detection strategies (Algorithms 2 and 3). We use the beats detected by our method in the synchronization with key video frames.

Next we discuss the video event detection and event synchronization.

# 4 Video Event Detection

We primarily detect no motion<sup>14</sup> ( $\nu^{nm}$  events) in the video. Given that  $\nu^{nm}$  and  $\nu^{tr}$  must alternate in the video, we then deduce the  $\nu^{tr}$  events. We detect no motion from the co-occurrence of the no motion in the RGB and Skeleton data of Kinect by (1) Frame Differences in RGB data and (2) Velocity acceleration of skeleton Joints.

<sup>&</sup>lt;sup>14</sup> Actually, slow or low motion in the video as cutoff by a threshold

Table 8. Comparison of beat detection results between Ellis' method [4] and our method for *Pakka Sollukattu* (data file = Pakka\_14\_HB1). For every *beat / bol* (col. 1) the range of estimated time as manually marked is shown under *Annotated Beat Range* (cols. 2-3). While Ellis' method detects all beats correctly (col. 4), it spuriously detects almost 100% (col. 5) and 200% (cols. 6-8) beats respectively within and outside the annotated time range. Hence it achieves 100% recall at 25% precision (127 beats detected for 32 correct beats). In contrast, our method detects 31 out of 32 beats correctly (col. 9) for 97% recall but detects only one spurious beat (col. 10) for 97% precision.

				[	Ellis' Method						Our Method	
					Within Range Outside Range				Withir	n Range		
Beat	Bol	Anno	tated		Correct	Spurious	S	purious	;	Correct	Spurious	
No.		Beat 1	Range		Beat	Beat		Beat		Beat	Beat	
(0)	(1)	(2)	(3)		(4)	(5)	(6)	(7)	(8)	(9)	(10)	
1	$_{\mathrm{ta}}$	2.160	2.642		2.182	2.490	2.798	3.082	3.366	2.180		
2	tei	3.481	4.088		3.654	3.938	4.226	4.558		3.634		
3	tei	4.855	5.426		4.894	5.226	5.558	5.906		4.988		
4	tat	6.194	6.747		6.242	6.578	6.910	7.234		6.312		
5	$_{\rm dhit}$	7.479	8.032		7.554	7.870	8.190	8.514		7.541		
6	tei	8.764	9.336		8.822	9.138	9.450	9.778		8.808		
7	tei	10.067	10.639		10.114	10.434	10.750	11.086		10.199		
8	tat	11.353	11.817		11.390	11.706	12.022	12.346		11.455		
9	$_{\mathrm{ta}}$	12.602	13.155		12.670	12.982	13.298	13.602		12.785		
10	tei	13.905	14.423		13.926	14.230	14.534	14.842		14.037		
11	tei	15.101	15.619		15.154	15.466	15.778	16.082		15.260		
12	tat	16.351	16.886		16.390	16.690	16.986	17.298		16.483		
13	$_{\rm dhit}$	17.564	18.100		17.610	17.898	18.186	18.490		17.669		
14	tei	18.760	19.296		18.790	19.102	19.410	19.734		18.778		
15	tei	19.974	20.545		20.030	20.326	20.622	20.918		20.149		
16	tat	21.170	21.670		21.218	21.506	21.798	22.102		21.208		
17	$_{\mathrm{ta}}$	22.312	22.884		22.402	22.686	22.974	23.278		22.499		
18	tei	23.562	24.097		23.610	23.906	24.206	24.506		23.602		
19	tei	24.740	25.347		24.806	25.106	25.410	25.718		24.868		
20	tat	25.990	26.507		26.018	26.318	26.614	26.906		26.110		
21	dhit	27.114	27.632		27.202	27.498	27.794	28.082		27.268		
22	tei	28.364	28.917		28.402	28.694	28.990	29.294		28.391		
23	tei	29.524	30.095		29.594	29.882	30.170	30.478		29.654		
24	tat	30.773	31.345		30.814	31.106	31.402	31.706		30.804		
25	$_{\mathrm{ta}}$	31.934	32.523		32.010	32.298	32.590	32.894		32.099		
26	tei	33.165	33.683		33.194	33.482	33.770	34.066		33.271		
27	tei	34.343	34.843		34.366	34.658	34.946	35.238		34.352	35.514	
28	tat	35.521	36.021		35.526	35.814	36.102	36.390				
29	dhit	36.610	37.128		36.678	36.958	37.242	37.534		36.743		
30	tei	37.806	38.324	T	37.834	38.118	38.406	38.698		37.945		
31	tei	38.966	39.466		38.998	39.282	39.570	39.866		39.112		
32	tat	40.145	40.644	T	40.190	40.510				40.263		

(All times are in sec)

Sollukattu	Actual	Slov	ver	Fas	ter	Strength	Estimated	Remarks
	Tempo	Estin	nate	Estin	Estimate		Tempo	
	Period	bpm	Period	bpm	Period		Period	
(0)	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)
Joining A	1.18	55.147	1.09	110.294	0.54	0.05	0.54	Wrong
Joining B	1.52	32.189	1.86	64.378	0.93	0.08	0.93	Right
Joining C	1.17	52.083	1.15	104.167	0.58	0.63	1.15	Wrong
Kartari Utsanga	1.07	59.055	1.02	118.110	0.51	0.41	0.51	Wrong
Kuditta Mettu	1.16	100.000	0.60	200.000	0.30	0.65	0.60	Wrong
Kuditta Nattal A	0.99	63.559	0.94	127.119	0.47	0.16	0.47	Wrong
Kuditta Nattal B	1.30	46.296	1.30	92.593	0.65	0.22	0.65	Wrong
Kuditta Tattal	1.21	101.351	0.59	202.703	0.30	0.74	0.59	Wrong
Natta	1.39	43.860	1.37	87.719	0.68	0.28	0.68	Wrong
Paikkal	1.58	38.660	1.55	77.320	0.78	0.11	0.78	Wrong
Pakka	1.21	100.000	0.60	200.000	0.30	0.66	0.60	Wrong
Sarika	0.93	61.983	0.97	123.967	0.48	0.68	0.97	Right
Tatta A	1.51	41.899	1.43	83.799	0.72	0.14	0.72	Wrong
Tatta B	1.36	22.189	2.70	44.379	1.35	0.01	1.35	Right
Tatta C	1.56	39.063	1.54	78.125	0.77	0.31	0.77	Wrong
Tatta D	1.35	45.455	1.32	90.909	0.66	0.19	0.66	Wrong
Tatta E	1.17	36.765	1.63	110.294	0.54	0.14	0.54	Wrong
Tatta F	1.21	48.387	1.24	96.774	0.62	0.65	1.24	Right
Tatta G	1.32	45.455	1.32	90.909	0.66	0.51	1.32	Right
Tei Tei Dhatta	1.41	66.964	0.90	133.929	0.45	0.32	0.45	Wrong
Tirmana A	1.23	47.468	1.26	94.937	0.63	0.06	0.63	Wrong
Tirmana B	1.22	50.000	1.20	100.000	0.60	0.13	0.60	Wrong
Tirmana C	1.46	90.361	0.66	180.723	0.33	0.87	0.66	Wrong

Table 9. Estimation of tempo period by Ellis' method [4]

(All times are in sec) ( $bpm \equiv beats \ per \ minute. \ Period = 60/bpm$ )

#### 4.1 Frame Differences in RGB Stream

Frame difference or image sequence difference method refers to a very small time intervals of the two images before and after the pixel based on the time difference, and then using a threshold to extract the image regions of the movement. The image is then binarized based on motion (marked as 1) and no motion (marked as 0). We sum the the non-zero pixels (having motion) present in the image and then label it as motion or no motion frame based on a threshold.

#### 4.2 Velocity-Acceleration in Skeleton Stream

We compute the velocity and acceleration for 4 joint points (Wrist, Elbow, Knee and Ankle) of the Kinect skeleton corresponding to every RGB frame. If the StartPoint is  $(x_1, y_1, z_1)$  and the EndPoint is  $(x_2, y_2, z_2)$  then the instantaneous velocity is  $v = (v_x, v_y, v_z) = velocity(x_2 - x_1, y_2 - y_1, z_2 - z_1)$  and the instanta-

Sollukattu		Ellis' N	Our M	$\mathbf{ethod}$			
		usi	usi	ng			
	Estima	$ted^a$	Give	n <sup>b</sup>	Given Ranges of <sup>c</sup>		
	Tempo F	Period	Tempo F	Period	Tempo Periods		
	Precision	Recall	Precision	Recall	Precision	Recall	
Joining A	38	83	71	83	86	100	
Joining B	73	92	54	58	100	100	
Joining C	63	95	100	70	100	100	
Kartari Utsanga	96	98	100	52	100	100	
Kuditta Mettu	25	100	50	100	81	81	
Kuditta Nattal A	37	96	40	25	71	92	
Kuditta Nattal B	74	96	93	58	100	100	
Kuditta Tattal	25	94	48	63	88	88	
Natta	50	100	100	94	81	81	
Paikkal	100	75	100	75	100	100	
Pakka	25	100	97	97	97	97	
Sarika	50	100	97	94	97	97	
Tatta A	39	100	88	58	100	75	
Tatta B	48	92	100	83	100	100	
Tatta C	68	100	86	57	75	100	
Tatta D	65	100	100	75	94	100	
Tatta E	18	100	75	100	65	92	
Tatta F	22	100	88	100	88	100	
Tatta G	30	100	91	71	100	100	
Tei Tei Dhatta	65	100	96	72	100	100	
Tirmana A	68	100	68	100	91	82	
Tirmana B	87	98	87	98	100	100	
Tirmana C	41	100	100	58	95	75	

Table 10. Comparison of Precision and Recall between Ellis' [4] and our methods

<sup>a</sup>: Original dynamic programming method of Ellis

<sup>b</sup>: Ellis' method where the actual tempo period has been set for each Sollukattu <sup>c</sup>: Our method where a common range of tempo periods are set for all

neous acceleration is  $a = (a_x, a_y, a_z) = acceleration(v_{x_2} - v_{x_1}, v_{y_2} - v_{y_1}, v_{z_2} - v_{z_1})$ . If acceleration |a| is less than a threshold then no motion is inferred.

Finally, a frame is marked with no motion  $(\nu^{nm})$  if it does not show symptoms of motion from frame difference as well as velocity-acceleration. The range of consecutive no motion frames forms  $\eta_{est}(\nu^{nm})$  (the frames preceding and following this range must have motion).

## 4.3 Results of Video Event Detection

Now we present the results for video event detection using our data set.

Video Data Set: Adavu's are captured at 30 fps by Microsoft Kinect XBox (Kinect 1.0) using a special purpose capture software nuiCapture [1]. Every

recorded file comprises RGB, depth, skeleton, and audio streams. For each of 50 variants of 15 Adavu's, we have recorded over 20 sessions each as performed by 7 dancers (4 female and 3 male) giving over 1000 performance videos to analyze. 10% of the data has so far been annotated<sup>15</sup> by experts at frame level. An example for annotated Audio-Visual Data of *Kuditta Mettu Adavu* is shown in Table 12.

**Result Analysis:** We compare the video events by using the above algorithms with the manually annotated video events. First, we get a sequence of no-motion frame ranges from the detection algorithm (as in the manual video annotation given in Table 5). Next, we determine the number of overlapped ranges between detected video (DV) and annotated video (AV) events and compute precision and recall of the detection as:

$$Precision = \frac{Number of overlapped ranges between DV and AV}{Number of DV events} * 100$$
$$Recall = \frac{Number of overlapped ranges between DV and AV}{Number of AV events} * 100$$

The results are given Table 11. If the precision and recall both are  $\geq 75\%$  then we mark it as *Good*, if their minimum is within 74-50% then we mark it as *Moderate*, otherwise mark the result as *Poor*. We achieve 84% accuracy for *Good* and *Moderate* quality detection of video events.

As expected, we achieve *Good* results where the distinction between key postures and transitions is clear in the dance sequence. In a few *Adavu*'s like *Kuditta Nattal 1, Kuditta Nattal 5*, and *Kuditta Tattal 1* the dancer holds the key postures in over only a few of frames (generally it is 15-20 frames, but in these cases it is down to 2-3 frames). Such key postures are missed out in detection especially because the estimated skeletons are not stable and well-formed. Thus the detection performance goes down from *Good* to *Poor* depending on the clarity of the key posture in the sequence itself.

## 5 Estimation of Event Synchronization

For a detected beat  $\alpha^{fp}$ , we have the estimated time-stamp  $\tau(\alpha^{fp})$  from Section 3.4. We convert this to frame number  $\eta(\alpha^{fp})$  of the video (using 30 fps). We use a buffer threshold of  $\pm 5$  frames to get the frame interval  $\eta_{est}(\alpha^{fp})$  of  $\alpha^{fp}$  as  $[\eta(\alpha^{fp}) - 5, \eta(\alpha^{fp}) + 5]$ . Similarly, for a detected no motion event  $\nu^{nm}$ , we have the estimated frame range as  $\eta_{est}(\nu^{nm})$  from Section 4.

Finally, the sync event  $\psi^{fb}$  is inferred as

$$\eta_{est}(\alpha^{fb}) \cap \eta_{est}(\nu^{nm}) \neq \phi$$

Synchronization in annotated audio and video events are shown in Table 12.

<sup>&</sup>lt;sup>15</sup> Part of this data set is available at: http://cse.iitkgp.ac.in/resgrp/hci/

Sr.	Adavu	Precision	Recall	Remarks	Sr.	Adavu	Precision	Recall	Remarks
1	Tatta 1	100.00	100.00	Good	26	Kuditta Nattal 6	57.14	100.00	Moderate
2	Tatta 2	88.89	100.00	Good	27	Kuditta Tattal 1	85.00	35.42	Poor
3	Tatta 3	80.00	100.00	Good	28	Paikkal 1	50.00	75.00	Moderate
4	Tatta 4	94.12	100.00	Good	29	Paikkal 2	80.00	100.00	Good
5	Tatta 5	90.48	95.00	Good	30	Paikkal 3	70.00	87.50	Moderate
6	Tatta 6	81.82	75.00	Good	31	Tei Tei Dhatta 1	71.43	62.50	Moderate
7	Tatta 7	100.00	92.86	Good	32	Tei Tei Dhatta 2	50.00	87.50	Moderate
8	Tatta 8	100.00	100.00	Good	33	Tei Tei Dhatta 3	50.00	12.50	Poor
9	Natta 1	77.78	87.50	Good	34	Katti or Kartari 1	61.54	100.00	Moderate
10	Natta 2	80.00	100.00	Good	35	Utsanga 1	100.00	75.00	Good
11	Natta 3	94.12	100.00	Good	36	Mandi 1	51.11	71.88	Moderate
12	Natta 4	37.84	87.50	Poor	37	Mandi 2	86.36	59.38	Moderate
13	Natta 5	82.35	87.50	Good	38	Sarrikkal 1	60.53	71.88	Moderate
14	Natta 6	93.75	93.75	Good	39	Sarrikkal 2	80.00	66.67	Moderate
15	Natta 7	100.00	50.00	Moderate	40	Sarrikkal 3	54.55	56.25	Moderate
16	Natta 8	100.00	58.33	Moderate	41	Tirmana 1	62.50	50.00	Moderate
17	Pakka 1	77.78	87.50	Good	42	Tirmana 2	47.37	50.00	Poor
18	Kuditta Mettu 1	80.00	50.00	Moderate	43	Tirmana 3	72.22	72.22	Moderate
19	Kuditta Mettu 2	100.00	50.00	Moderate	44	Sarika 1	90.91	62.50	Moderate
20	Kuditta Mettu 3	87.50	82.35	Good	45	Sarika 2	92.31	75.00	Good
21	Kuditta Nattal 1	85.71	75.00	Good	46	Sarika 3	100.00	100.00	Good
22	Kuditta Nattal 2	91.67	78.57	Good	47	Sarika 4	57.14	50.00	Moderate
23	Kuditta Nattal 3	72.73	66.67	Moderate	48	Joining 1	75.00	100.00	Good
24	Kuditta Nattal 4	50.00	36.36	Poor	49	Joining 2	33.33	33.33	Poor
25	Kuditta Nattal 5	80.00	28.57	Poor	50	Joining 3	33.33	40.00	Poor

 Table 11. Results of Video Event Detection

 Table 12. Annotation of Audio-Visual Data of Kuditta Mettu Adavu

	A	udio An	Video	Annotation		
	(In Tir	ne (Sec))	(In Fra	ame #)	(In	Frame #)
Events	Start	End	$\mathbf{S} \mathbf{t} \mathbf{a} \mathbf{r} \mathbf{t}$	End	$\mathbf{S} \mathbf{t} \mathbf{a} \mathbf{r} \mathbf{t}$	End
$\nu_1^{nm} \ [\alpha_1^{fb}$ (tei	)] 2.681	3.218	80	97	70	99
$\nu_2^{nm} [\alpha_2^{fb}]$ (has	t)] 3.912	4.247	117	127	104	124
$\nu_3^{nm} \ [\alpha_3^{fb}(\text{tei}$	)] 5.108	5.541	153	166	146	172
$\nu_4^{nm} \left[ \alpha_4^{fb}(\mathrm{hi}) \right]$	] 6.269	6.681	188	200	177	191
$\nu_5^{nm} \ [\alpha_5^{fb}$ (tei	)] 7.523	7.975	226	239	215	245
$\nu_6^{nm} [\alpha_6^{fb}(\text{has})]$	t)] 8.742	9.125	262	274	250	262
$\nu_7^{nm} [\alpha_7^{fb} (\text{tei}$	)] 9.891	10.375	297	311	288	314
$\nu_8^{nm} \left[ \alpha_8^{fb} (\mathrm{hi}) \right]$	] 11.064	11.563	332	347	318	345
$\nu_9^{nm} \ [\alpha_9^{fb}$ (tei	)] 12.271	12.698	368	381	359	386
$\nu_{10}^{nm} \left[\alpha_{10}^{fb}\right]$ (has	t)] 13.386	13.819	402	415	391	410
$\nu_{11}^{nm} \left[ \alpha_{11}^{fb} (\text{tei}$	)] 14.512	14.969	435	449	430	451
$\nu_{12}^{nm}  [\alpha_{12}^{fb}(\text{hi})$	] 15.603	16.109	468	483	456	470
$\nu_{13}^{nm} \left[\alpha_{13}^{fb}\right]$ (tei	)] 16.764	17.201	503	516	493	520
$\nu_{14}^{nm}  [\alpha_{14}^{fb} (hat$	t)] 17.902	18.302	537	549	526	542
$\nu_{15}^{nm} \left[\alpha_{15}^{fb}\right]$ (tei	)] 19.028	19.476	571	584	565	587
$\nu_{16}^{nm}  [\alpha_{16}^{fb}(\text{hi})$	] 20.178	20.630	605	619	591	620

#### 5.1 Results of Event Synchronization

After audio and video event detection we get time-stamp of beats from the audio signal and range of Key Posture from the video stream. Next we compute the quality of the match using the following measures:

Matching Detected Video (DV) events against Annotated Audio (AA) events:

$$Measure of Match (DV-AA) = \frac{Number of matched DV and AA events}{Number of AA Events} *100$$

Matching Detected Video (DV) events against Detected Audio (DA) events:

$$Measure of Match (DV-DA) = \frac{Number of matched DV and DA events}{Number of DA Events} *100$$

Detected audio and video events of *Kuditta Mettu 3 Adavu* are shown in Table 13. In 2 out of the 16 events, there is no overlap. Hence, we achieve 87.5% sync between the DA and DV events.

		Audio Time to	Video	Frames
Events	Detected Beats	Video Frame	Start	End
$\nu_1^{nm} \left[ \alpha_1^{fb}(\text{tei}) \right]$	2.742	82	78	83
$\nu_2^{nm} \ [\alpha_2^{fb}(hat)]$	3.964	119	95	119
$\nu_3^{nm} \left[ \alpha_3^{fb}(\text{tei}) \right]$	4.798	144	143	150
$\nu_4^{nm} \left[ \alpha_4^{fb}(\text{hi}) \right]$	6.280	188	157	198
$\nu_5^{nm} \left[ \alpha_5^{fb}(\text{tei}) \right]$	7.215	216	215	247
$\nu_6^{nm} \ [\alpha_6^{fb}(hat)]$	8.753	263	252	265
$\nu_7^{nm} \left[ \alpha_7^{fb} (\text{tei}) \right]$	9.600	288	289	299
$\nu_8^{nm} \left[ \alpha_8^{fb}(\text{hi}) \right]$	11.156	<u>335</u>	<u>303</u>	<u>330</u>
$\nu_9^{nm} \ [\alpha_9^{fb}(\text{tei})]$	12.333	370	364	389
$\nu_{10}^{nm} ~ [\alpha_{10}^{fb}(\text{hat})]$	13.485	405	392	405
$\nu_{11}^{nm} \left[ \alpha_{11}^{fb} (\text{tei}) \right]$	14.566	437	428	437
$\nu_{12}^{nm}  \left[ \alpha_{12}^{fb}({\rm hi}) \right]$	15.624	469	442	481
$\nu_{13}^{nm} \left[\alpha_{13}^{fb}(\text{tei})\right]$	16.776	503	500	539
$\nu_{14}^{nm} \left[ \alpha_{14}^{fb}(\text{hat}) \right]$	17.973	<u>539</u>		
$\nu_{15}^{nm} \left[\alpha_{15}^{fb}(\text{tei})\right]$	19.030	571	565	572
$\nu_{16}^{nm}  \left[ \alpha_{16}^{fb}(\text{hi}) \right]$	20.189	606	575	621

Table 13. Detected Audio & Video Events of Kuditta Mettu

**Result Analysis:** In Table 14 we present the summary of sync results and analyze the quality of sync. We also achieve 72% accuracy of *Good* (DV-DA > 75%) or *Moderate* (50% < DV-DA < 75%) synchronization. We explain the reasons behind the poor results below:

- 1. We detect motion or no-motion of a frame from the change in the current frame with respect to the previous frame. If the change in the consecutive frames are very low then very slow motion gets falsely detected as no-motion. Hence, number of detected Key Posture is becomes more than number of annotated key postures. This is happening in *Paikkal 3*.
- 2. In some Adava's like Kuditta Nattal 4, Tei Tei Dhatta 3, Kuditta Nattal 5, Natta 7 and Natta 8 the dancer holds the key posture for very small span of time. Hence, the Key Posture detection fails for the reasons explained in Section 4.3 and less Key Postures are detected than the actual annotated.

Sr.	Adavu	DV-AA	DV-DA	$\mathbf{Remark}$	$\mathbf{Sr.}$	Adavu	DV-AA	DV-DA	$\mathbf{Remark}$
1	Tatta 1	100.00	100.00	Good	26	Kuditta Nattal 6	100.00	41.94	Poor
2	Tatta 2	100.00	100.00	Good	27	Kuditta Tattal 1	35.42	31.25	Poor
3	Tatta 3	100.00	100.00	Good	28	Paikkal 1	75.00	56.25	Moderate
4	Tatta 4	100.00	100.00	Good	29	Paikkal 2	56.25	56.25	Moderate
5	Tatta 5	93.75	94.12	Good	30	Paikkal 3	31.25	56.25	Moderate
6	Tatta 6	75.00	58.82	Moderate	31	Tei Tei Dhatta 1	62.50	62.50	Moderate
7	Tatta 7	92.86	81.25	Good	32	Tei Tei Dhatta 2	87.50	68.75	Moderate
8	Tatta 8	100.00	100.00	Good	33	Tei Tei Dhatta 3	12.50	12.50	Poor
9	Natta 1	87.50	81.25	Good	34	Katti or Kartari 1	100.00	54.17	Moderate
10	Natta 2	100.00	100.00	Good	35	Utsanga 1	50.00	29.17	Poor
11	Natta 3	100.00	93.75	Good	36	Mandi 1	64.58	87.23	Good
12	Natta 4	90.63	81.25	Good	37	Mandi 2	39.58	40.43	Poor
13	Natta 5	87.50	75.00	Good	38	Sarrikkal 1	52.08	68.09	Moderate
14	Natta 6	93.75	87.50	Good	39	Sarrikkal 2	37.00	38.31	Poor
15	Natta 7	50.00	50.00	Moderate	40	Sarrikkal 3	56.25	65.96	Moderate
16	Natta 8	58.33	43.75	Poor	41	Tirmana 1	50.00	72.73	Moderate
17	Pakka 1	50.00	65.63	Moderate	42	Tirmana 2	45.83	62.50	Moderate
18	Kuditta Mettu 1	50.00	56.25	Moderate	43	Tirmana 3	58.33	59.09	Moderate
19	Kuditta Mettu $2$	81.25	50.00	Moderate	44	Sarika 1	62.50	68.75	Moderate
20	Kuditta Mettu 3	75.00	87.50	Good	45	Sarika 2	75.00	37.50	Poor
21	Kuditta Nattal 1	54.55	45.16	Poor	46	Sarika 3	53.13	56.25	Moderate
22	Kuditta Nattal 2	55.00	38.71	Poor	47	Sarika 4	50.00	28.13	Poor
23	Kuditta Nattal 3	50.00	41.94	Poor	48	Joining 1	100.00	85.71	Good
24	Kuditta Nattal 4	26.67	31.25	Poor	49	Joining 2	100.00	87.50	Good
25	Kuditta Nattal 5	26.67	18.75	Poor	50	Joining 3	37.50	56.25	Moderate

Table 14. Results of Sync Events in percentage of Match

## 6 Conclusions

This paper is the maiden approach to characterize the *Bharatanatyam* dance form and attempt multimedia analytics for Kinect data of *Bharatanatyam Adavu*'s. In the process we make the following contributions:

1. We characterize the events of *Bharatanatyam Adavu*'s for automated analysis. First we analyze and document the structure of its music – understanding

the pattern of beats and bol's in depth. Next we outline the characterization of its video in terms of key postures. Finally, we identify core synchronization issues in an Adavu.

2. We present a simple yet effective algorithm to detect beats in *Sollukattu*'s. We validate the results against annotated data. Overall we achieve 94% accuracy.

We compare our results against the Ellis' algorithm [4]. Under similar conditions, our algorithm performs better. We show that the correct estimation of tempo period is crucial for accurate beat detection and the same remains elusive for now.

- 3. We present algorithms to detect no-motion video events and achieve 84% accuracy for it.
- 4. In terms of audio-video sync, we achieve 72% accuracy.
- 5. No annotated data of *Sollukattu*'s and *Adavu*'s is available for research. We have recorded 6 six sets of all 23 *Sollukattu*'s and 20 sessions of all 50 variants of 15 *Adavu*'s. 30% of audio and 10% of video data have already been annotated by experts.

The paper also raises several questions including:

1. Beat Detection and Marking: From the characterization we know that most beats are accompanied by a *bol*. Since the current approach is based on onsets, it ignores the *bol*'s. We can create a vocab of *bol*'s, detect these as utterances, and correspond with the onsets to achieve near 100% accuracy. Once *bol*'s are known, the same can be marked on the stream. Half beats also need to be detected.

Information of *bol*'s can also be used to estimate the tempo period accurately which, as discussed, is a critical factor in beat detection.

Estimating lead / lag between instrumental and vocal sound and the uniformity of beat-to-beat time gaps would be key problems for a *Sollukattu*.

- 2. Detection of Key Frames and Audio-guided Segmentation of Adavu's: The paper presents an important characterization of the video of Adavu in terms of K- and T-Frames. These can be further characterized in terms of motion parameters. Based on the marked beats and bol's, the video may be segmented at approximate K-Frames and then refined with motion estimates.
- 3. *Synchronization Issues*: Based on the solution of the above problems, several synchronization issues as discussed in Section 2.4 may be attempted.

It may be reiterated that the characterization of *Adavu*'s and detection of beats in *Sollukattu*'s have several applications including music segmentation, music video segmentation, estimating the synchronization of the postures with the musical beats, automatic tagging of rhythm metadata of music, synchronization correction, and the like. These can be attempted in future.

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